

$$2(x - \frac{3}{2})$$

c.  $(8x^4 - 16x^3 + 16x^2 - 27x + 18) \div (2x - 3)$

$$\begin{array}{r} \frac{3}{2} \\[-1ex] | \quad 8 \quad -16 \quad 16 \quad -27 \quad 18 \\[-1ex] \downarrow \quad 12 \quad -6 \quad 15 \quad -18 \\[-1ex] \hline 8 \quad -4 \quad 10 \quad -12 \quad 0 \end{array}$$

?  $(2x-3) \times 8x^3 - 4x^2 + 10x - 12$  ?  
 $(x - \frac{3}{2}) \times 8x^3 - 4x^2 + 10x - 12$   
 $(2x-3)(4x^3 - 2x^2 + 5x - 6)$

$\boxed{4x^3 - 2x^2 + 5x - 6}; x \neq \frac{3}{2}$

d.  $(15x^4 - x^3 - 11x^2 + 17x + 9) \div (5x + 3)$

$$\begin{array}{r} \frac{3}{5} \\[-1ex] | \quad 15 \quad -1 \quad -11 \quad 17 \quad 9 \\[-1ex] \downarrow \quad -9 \quad 6 \quad 3 \quad -12 \\[-1ex] \hline 15 \quad -10 \quad -5 \quad 20 \quad \boxed{3} \end{array}$$

$3x^3 - 2x^2 - x + 4 + \frac{-3}{5x+3}$

$(5x+3)(3x^3 - 2x^2 - x + 4) - 3$  Factored form

Example 3:

division

a. Use synthetic substitution to evaluate the function.

f(-2) for  $f(x) = x^4 - 3x^3 + 7x^2 - 20$

remainder th.  
f(-2) =  $(-2)^4 - 3(-2)^3 + 7(-2)^2 - 20$   
= 48

Synthetic ÷  $\begin{array}{r} \boxed{-2} \quad | \quad 1 \quad -3 \quad 7 \quad 0 \quad -20 \\ \downarrow \quad \quad \quad -2 \quad 10 \quad -34 \quad 68 \\ \hline 1 \quad -5 \quad 17 \quad 34 \quad \boxed{48} \end{array}$

b. Determine  $k$  so that  $g(x) = 2x^3 + 5x^2 + kx - 16$  has  $x - 2$  as a factor.

or  $\begin{array}{r} \boxed{2} \quad \underline{\boxed{2}} \quad \underline{\boxed{5}} \quad K \quad -16 \\ \downarrow \quad \quad \quad 4 \quad 18 \quad \underline{2k+36} \\ \hline 2 \quad 9 \quad K+18 \quad \underline{2k+20} \end{array}$   $2k+20=0$   
 $K=-10$

$2(2)^3 + 5(2)^2 + K(2) - 16 = 0$   
 $16 + 20 + 2K = 16$   
 $K = -10$

We will now do #7, 13, 19, 25, 45(a,b), 69, 84 (see below) as classwork. It is due IN CLASS.

7. Use long division to divide  $(4x^3 - 7x^2 - 11x + 5) \div (4x + 5)$ .
13. Use long division to divide  $(6x^3 + 10x^2 + x + 8) \div (2x^2 + 1)$ .
19. Use synthetic division to divide  $(3x^3 - 17x^2 + 15x - 25) \div (x - 5)$ .
25. Use synthetic division to divide  $(5x^3 - 6x^2 + 8) \div (x - 4)$ .
45. Use synthetic division to find each function value.  $f(x) = 4x^3 - 13x + 10$ .
  - a.  $f(1)$
  - b.  $f(-2)$

69. Simplify the rational expression  $\frac{4x^3 - 8x^2 + x + 3}{2x - 3}$  by using long division or synthetic division.

84. Find the constant  $c$  such that the denominator will divide evenly into the numerator for the rational expression  $\frac{x^3 + 4x^2 - 3x + c}{x - 5}$ .

## 2.3 Answers

⑦  $x^2 - 3x + 1; x \neq -\frac{5}{4}$

⑬ 
$$\begin{array}{r} 3x+5 \\ \hline 2x^2 + 0x + 1 \longdiv{6x^3 + 10x^2 + x + 8} \\ - \cancel{6x^3} + \cancel{0x^2} + 3x \\ \hline 10x^2 - 2x + 8 \\ 10x^2 + 0x + 8 \\ \hline -2x + 8 \end{array}$$

$$3x+5 + \frac{-2x+8}{2x^2+1}$$

$2x^2+1 \neq 0$   
No restrictions

⑯ 5] 
$$\begin{array}{r} 3 & -17 & 15 & -25 \\ \downarrow & 15 & -10 & 25 \\ \hline 3 & -2 & 5 & 10 \end{array}$$

$3x^2 - 2x + 5; x \neq 5$

⑰ 4] 
$$\begin{array}{r} 5 & -6 & 0 & 8 \\ \downarrow & 20 & 56 & 24 \\ \hline 5 & 14 & 56 & 232 \end{array}$$

$5x^2 + 14x + 56 + \frac{232}{x-4}; x \neq 4$

④5) a)  $f(1) = 1$       b)  $f(-2) = 4$

⑥9)  $2x^2 - x - 1 ; x \neq \frac{3}{2}$

⑧4)  $(s)^3 + 4(s)^2 - 3(s) + C = 0$   
 $125 + 100 - 15 + C = 0$   
 $C = -210$

or

$$\begin{array}{r} 5 | & 1 & 4 & -3 & C \\ & \downarrow & 5 & 45 & 210 \\ \hline & 1 & 9 & 42 & 0 \end{array}$$

$C = -210$