

To complete our study of differentiation and inverse functions, we will now focus on taking the derivatives of the six inverse trigonometric functions.

Derivatives of Basic Inverse Trigonometric Functions

$$\frac{d}{dx} [\arcsin x] = \frac{1}{\sqrt{1-x^2}}$$

$$\frac{d}{dx} [\arccos x] = -\frac{1}{\sqrt{1-x^2}}$$

$$\frac{d}{dx} [\arctan x] = \frac{1}{1+x^2}$$

$$\frac{d}{dx} [\operatorname{arccot} x] = \frac{1}{1+x^2}$$

$$\frac{d}{dx} [\operatorname{arcsec} x] = \frac{1}{|x|\sqrt{x^2-1}}$$

$$\frac{d}{dx} [\operatorname{arccsc} x] = -\frac{1}{|x|\sqrt{x^2-1}}$$

THEOREM: Derivatives of the Six Inverse Trigonometric Functions (Chain Rule)

Let u be a function of x .

$$\frac{d}{dx} [\arcsin u] = \frac{u'}{\sqrt{1-u^2}}$$

$$\frac{d}{dx} [\arccos u] = \frac{-u'}{\sqrt{1-u^2}}$$

$$\frac{d}{dx} [\arctan u] = \frac{u'}{1+u^2}$$

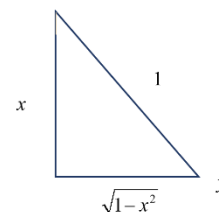
$$\frac{d}{dx} [\operatorname{arccot} u] = \frac{-u'}{1+u^2}$$

$$\frac{d}{dx} [\operatorname{arcsec} u] = \frac{u'}{|u|\sqrt{u^2-1}}$$

$$\frac{d}{dx} [\operatorname{arccsc} u] = \frac{-u'}{|u|\sqrt{u^2-1}}$$



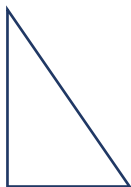
Let $y = \arcsin x$. How could we find $\frac{dy}{dx}$ without using an inverse trigonometric function?



Example 1: Find each of the following derivatives.

a. $\frac{d}{dx} [\arcsin(2x)]$

Long Method



Derivative Rule

b. $\frac{d}{dx} [\arctan(3x)]$

c. $\frac{d}{dx}[\tan^{-1} \sqrt{x}]$

d. $\frac{d}{dx}[\sec^{-1}(e^{2x})]^2$